

LEARNING CENTRE	TEST PAPER	MATHEMATICS
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01:-The domain of the function $f(x) = \sin^{-1}\left(\log_2\left(\frac{x^2}{2}\right)\right)$ is

- (A) $[-2, 2]$ (B) $[-2, -1]$ (C) $[1, 2]$ (D) $[-2, -1] \cup [1, 2]$

02:-The coordinates of the point on the parabola $y = x^2 + 7x + 2$, which is nearest to the straight line $y = 3x - 3$ are

- (A) $(-2, -8)$ (B) $(1, 10)$ (C) $(2, 20)$ (D) $(-1, -4)$

03:-From origin, chords are drawn to the circle $x^2 + y^2 - 2y = 0$. The locus of the middle points of these chords is

- (A) $x^2 + y^2 - y = 0$ (B) $x^2 + y^2 - x = 0$ (C) $x^2 + y^2 - 2x = 0$ (D) $x^2 + y^2 - x - y = 0$

04:-If $|z - 3i| = 3$, (where $i = \sqrt{-1}$) and $\arg z \in (0, \pi/2)$, then $\cot(\arg(z)) - \frac{6}{z}$ is equal to

- a) 0 b) $-i$ c) i d) none of these

05:-If $y = (\sin^{-1} x)^2 + (\cos^{-1} x)^2$, then $(1 - x^2) \frac{d^2 y}{dx^2} - x \frac{dy}{dx} =$

- A) -4 B) 4 C) 2 D) -2

06:-For each real number x such that $-1 < x < 1$, let $A(x)$ be the matrix $(1-x)^{-1} \begin{bmatrix} 1 & -x \\ -x & 1 \end{bmatrix}$ and $z = \frac{x+y}{1+xy}$.

Then,

- (A) $A(z) = A(x) + A(y)$ (B) $A(z) = A(x) [A(y)]^{-1}$
(C) $A(z) = A(x) A(y)$ (D) $A(z) = A(x) - A(y)$

07:-If matrix $A = [a_{ij}]_{3 \times 3}$, matrix $B = [b_{ij}]_{3 \times 3}$ where $a_{ij} + a_{ji} = 0$ and $b_{ij} - b_{ji} = 0$, then $A^4 \cdot B^3$ is

- (A) skew-symmetric matrix (B) singular (C) symmetric (D) zero matrix

08- The Cartesian equation of the plane passing through the line of intersection of the planes $r.(2i - 3j + 4k) = 1$ and $r.(i - j) + 4 = 0$ and perpendicular to the plane $r.(2i - j + k) + 8 = 0$ is

- (A) $3x - 4y + 4z = 5$ (B) $x - 2y + 4z = 3$
(C) $5x - 2y - 12z + 47 = 0$ (D) $2x + 3y + 4 = 0$

- 09:-Let $\vec{r}, \vec{a}, \vec{b}$ & \vec{c} be four non-zero vector such that $\vec{r} \cdot \vec{a} = 0, |\vec{r} \times \vec{b}| = |\vec{r}| |\vec{b}|, |\vec{r} \times \vec{c}| = |\vec{r}| |\vec{c}|$, then $[abc] =$
 (A) $|a| |b| |c|$ (B) $- |a| |b| |c|$ (C) 0 (D) none of these

- 10:-If $\int \frac{\sqrt{\cos 2x}}{\sin x} dx = -\log \left| \cot x + \sqrt{\cot^2 x - 1} \right| + A + C$, then A is equal to

- (a) $\frac{1}{\sqrt{2}} \log \left| \frac{\sqrt{2} + \sqrt{1 - \tan^2 x}}{\sqrt{2} - \sqrt{1 - \tan^2 x}} \right|$ (b) $\frac{1}{\sqrt{2}} \log \left| \frac{\sqrt{2} + \sqrt{1 - \sec^2 x}}{\sqrt{2} - \sqrt{1 - \sec^2 x}} \right|$
 (c) $\frac{1}{\sqrt{2}} \log \left| \frac{\sqrt{2} + \sqrt{1 - \sin^2 x}}{\sqrt{2} - \sqrt{1 - \sin^2 x}} \right|$ (d) None of these

- 11:-The area of the figure bounded by the straight lines $x=0, x=2$ and the curves $y=2^x, y=2x-x^2$, is

- (a) $\left(\frac{4}{\log 2} + \frac{8}{3} \right) sq. units$ (b) $\left(\frac{4}{\log 2} - \frac{8}{3} \right) sq. units$ (c) $\left(\frac{8}{\log 3} - \frac{4}{3} \right) sq. units$ (d) $\left(\frac{3}{\log 2} - \frac{4}{3} \right) sq. units$

- 12:-If $f(x)$ is a function satisfying $f(x+y) = f(x)f(y)$ for all $x, y \in N$ such that $f(1) = 3$ and

$$\sum_{x=1}^n f(x) = 120, \text{ then the value of } n \text{ is}$$

- (a) 4 (b) 5 (c) 6 (d) None of these

- 13:-A bag contains a white and b black balls. Two players A and B alternately draw a ball from the bag, replacing the ball each time after the draw. A begins the game. If the probability of A winning (that is drawing a white ball) is twice the probability of B winning (that is drawing a black ball), then the ratio $a:b$ is equal to

- (a) 1:2 (b) 2:1 (c) 1:1 (d) Neither one – one nor onto

14:-The value of $\int_0^1 \frac{x^4 (1-x)^4}{1+x^2} dx$ is

- (a) 0 (b) $\frac{2}{105}$ (c) $\frac{22}{7} - \pi$ (d) $\frac{71}{15} - \frac{3\pi}{2}$

15:-The median of a set of 11 distinct observations is 20.5. If each of the last 5 observations of the set is increased by 4, then the median of the new set

- (a) is increased by 2 (b) is decreased by 2
(c) is two times the original a median (d) remains the same as that of the original set

16:-Solution of the differential equation $\frac{\sqrt{x} dx + \sqrt{y} dy}{\sqrt{x} dx - \sqrt{y} dy} = \sqrt{\frac{y^3}{x^3}}$ is given by

(a) $\frac{3}{2} \log \left(\frac{y}{x} \right) + \log \left| \frac{x^{3/2} + y^{3/2}}{x^{3/2}} \right| + \tan^{-1} \left(\frac{y}{x} \right)^{3/2} + c = 0$

(b) $\frac{2}{3} \log \left(\frac{y}{x} \right) + \log \left| \frac{x^{3/2} + y^{3/2}}{x^{3/2}} \right| + \tan^{-1} \left(\frac{y}{x} \right) + c = 0$

(c) $\frac{2}{3} \log \left(\frac{y}{x} \right) + \log \left| \frac{x+y}{x} \right| + \tan^{-1} \left(\frac{y^{3/2}}{x^{3/2}} \right) + c = 0$

(d) I is false, II is true

17:-The integer $\int_{-1/2}^{1/2} \left[[x] + \log \left(\frac{1+x}{1-x} \right) \right] dx$ is equal to

- (a) $-\frac{1}{2}$ (b) 0 (c) 1 (d) $2 \log \frac{1}{2}$

18:-A function $y = f(x)$ has a second order derivative $f''(x) = 6(x-1)$. If its graph passes through the point (2, 1) and at that point the tangent to the graph is $y = 3x - 5$, then the function is

- (a) $(y-1)^3$ (b) $(y+1)^3$ (c) $(x+1)^2$ (d) $(x-1)^2$

19:-The sum of n terms of the following series $1 + (1 + x) + (1 + x + x^2) + \dots$ will be

- (a) $\frac{1 - x^n}{1 - x}$ (b) $\frac{x(1 - x^n)}{1 - x}$ (c) $\frac{n(1 - x) - x(1 - x^n)}{(1 - x)^2}$ (d) None of these

20:- At a point P on the ellipse $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ tangent PQ is drawn. If the point Q be at a distance $\frac{1}{p}$ from the point P , where P is distance of the tangent from the origin, then the locus of the point Q is

- (a) $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1 + \frac{1}{a^2b^2}$ (b) $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1 - \frac{1}{a^2b^2}$
 (c) $\frac{x^2}{a^2} + \frac{y^2}{b^2} = \frac{1}{a^2b^2}$ (d) $\frac{x^2}{a^2} - \frac{y^2}{b^2} = \frac{1}{a^2b^2}$

21:-Let $\alpha, \beta \in R$ be such that $\lim_{x \rightarrow 0} \frac{x^2 \sin(\beta x)}{\alpha x - \sin x} = 1$. Then $6(\alpha + \beta)$ equals

22:-The smallest value of k , for which both the roots of the equation

$$x^2 - 8kx + 16(k^2 - k + 1) = 0$$

are real, distinct and have values at least 4, is

23:-The positive integer value of $n > 3$ satisfying the equation $\frac{1}{\sin\left(\frac{\pi}{n}\right)} = \frac{1}{\sin\left(\frac{2\pi}{n}\right)} + \frac{1}{\sin\left(\frac{3\pi}{n}\right)}$ is.....

24:-The number of values of θ in the interval $\left(-\frac{\pi}{2}, \frac{\pi}{2}\right)$ such that $\theta \neq \frac{n\pi}{5}$ for $n = 0, \pm 2$ and $\tan \theta = \cot 5\theta$ as well as $\sin 2\theta = \cos 4\theta$ is.....

25:-Number of ordered triplets of natural number (a, b, c) for which $abc \leq 11$ is